



UiO : **Universitetet i Oslo**

Directed Acyclic Graphs

Cecilie Dahl
Researcher
Department of Community Medicine and Global Health
University of Oslo
cecilie.dahl@medisin.uio.no



Outline- 3 hour session

- Why do we need DAGs?
- Short- Need to know
- Analyzing a DAG (with examples)
- Daggity- the «easy way» to draw and analyze a DAG

- Practice drawing your own DAGs, discussion

WHY DO WE NEED DAGS?

Why causal graphs (DAGs)?

- Estimate effect of **exposure** on **disease** (causal relation)
- **Problem**
 - Association measures are biased
- DAGs help in :
 - Understanding
 - Confounding, selection bias, mediation
 - Analysis
 - Adjust or not
 - Discussion
 - Precise statement of prior assumptions

Criteria for a variable to be a confounder:

1. Associated with the exposure in the source population
2. Associated with the outcome (in the unexposed)
3. Not on the causal pathway between exposure and outcome

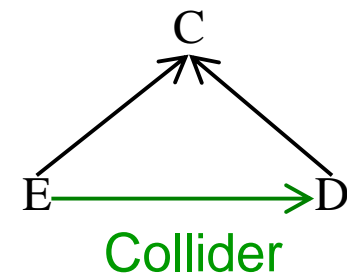
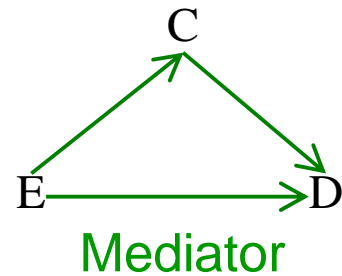
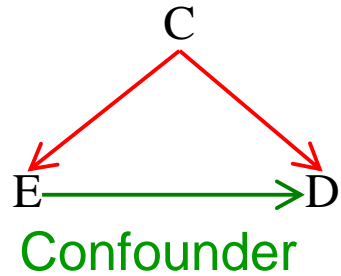
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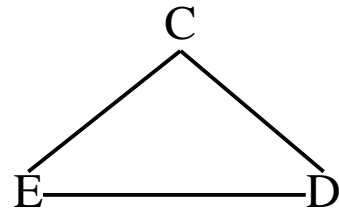
Not a sufficient definition

Adjust for C: cause versus association

Cause:



Association:



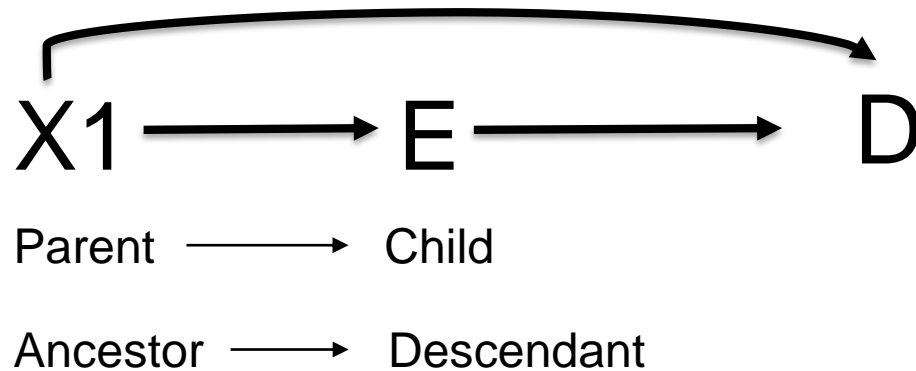
Statistical criteria:
 likelihood ratio, AIC, 10% change in estimate
 cannot differentiate between
 Confounder, Mediator or Collider

Need causal model to do a proper analysis

SHORT- NEED TO KNOW

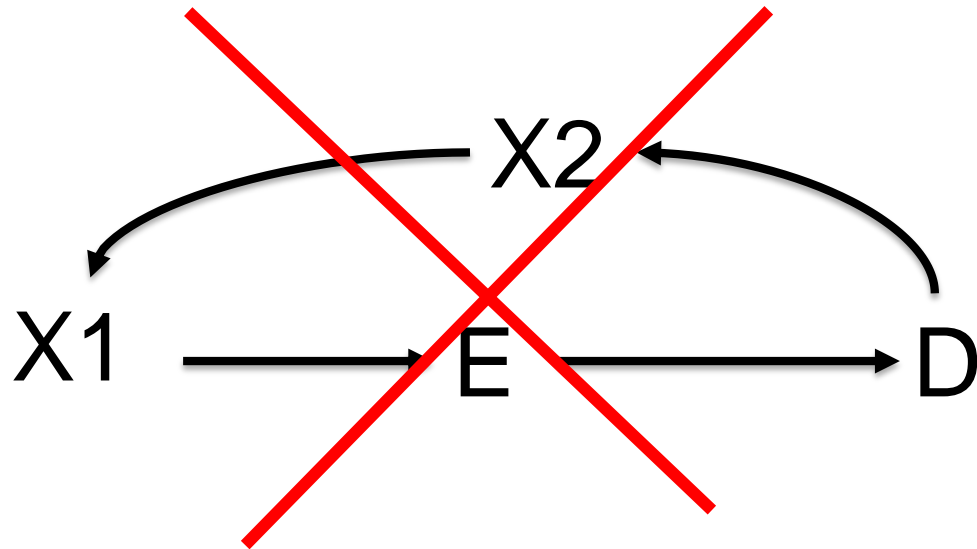
Time

- Time flows from left to right, and thus X1 is temporally prior to E and D , and E is temporally prior to Y



Acyclic

- Arrows in series cannot lead back to the same node (ACYCLIC)



Components

- Variables represented as «nodes» or «vertices»
- Arrows (edges) between variables represent causal effects
 - Depicting the *existence*, but *not the strength* of causal relationships (nor whether it is positive or negative)
 - Causation vs. Association paths
- Omission of an arrow is a stronger claim than the inclusion of an arrow

Causation vs. Association paths



E and D are
associated through
X1

X1 is a cause of E and D

Complete DAG?

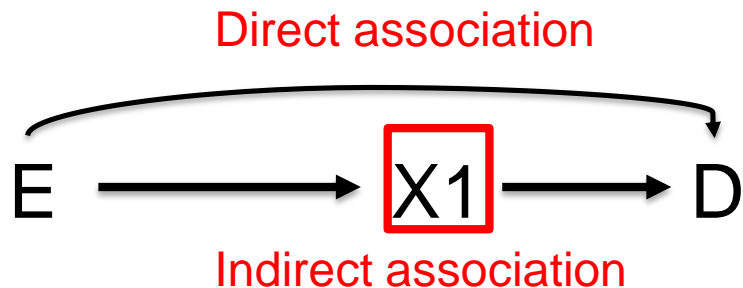
- Is the DAG a «complete view of the causal structure of reality»
 - Did we include all unmeasured variables (**U**)?
 - A DAG should also include these if they are part of the causal structure
 - Did we include all **common ancestors** of two variables?
 - Did we include all the arrows?
 - **Absence of an arrow is a strong statement**

ANALYZING A DAG

3 reasons why two variables may be associated

- One causes the other
- They share common causes
- They share a common effect and the analysis is restricted to certain level of that common effect (or of its descendants)

Conditioning on a mediator



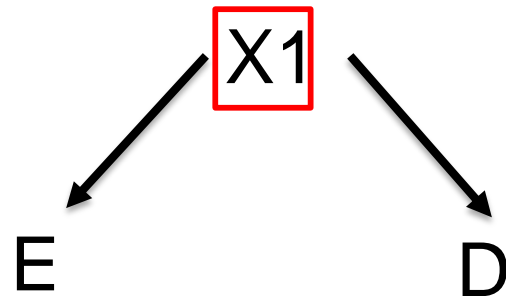
Conditioning blocks the indirect path- only direct association left.

May require special «mediation analysis»

Example: Aspirin (E) affects risk of heart disease (D) through reducing platelet aggregation (X1)

Conditioning on a common cause

- Confounding



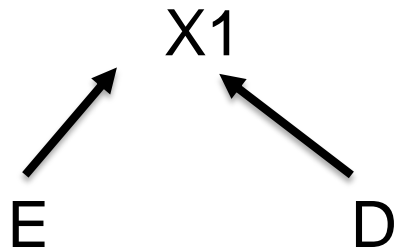
Example: Carrying a lighter (E) is associated with lung cancer (D). Smoking status (X1) is the underlying cause of both

Unconditioned-
Information on E could give information on E through X1

Conditioning-
Restricting $X1=1$ blocks all variation in E, i.e. variation in E gives no information in D

Conditioning on a common effect

- Selection bias
- Collider-stratification bias
- Bias due to conditioning on a collider

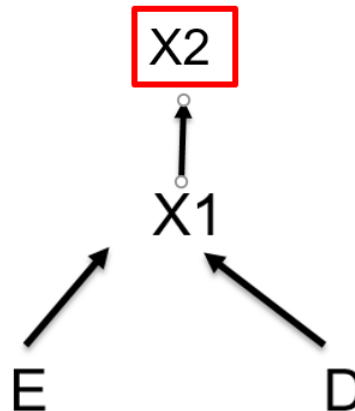
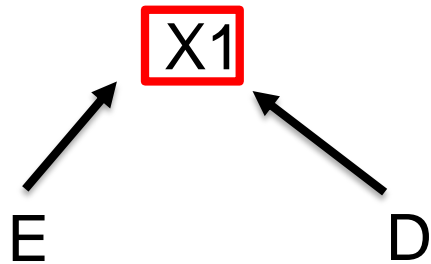


Information on E does not give information on D.

Example: A gene (E) and smoking status (D) are independent causes of hearth disease (X1)

Conditioning on a common effect

- Selection bias
- Collider-stratification bias
- Bias due to conditioning on a collider



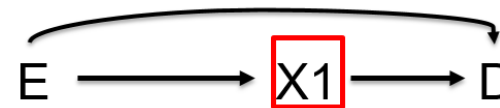
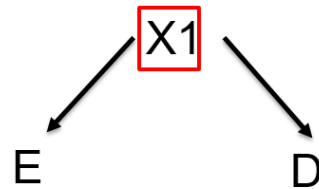
Conditioning on $X1=1$ or $X1=0$:
Information on E **does** give information on D.
- If E and D are the only two causes of X1, conditioning on $X1=1$ means that if and $E=0$, then D **has to** be=1

\perp = independent

D- separation

- Conditional independence
- Simply means that one variable (E) is independent of another variable (D), given another variable (X1) or a set of other variables (X1-X_t).

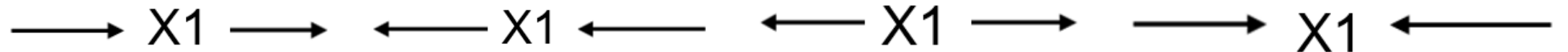
$E \perp D \mid X1$



- The opposite is «d-connected»

How to identify and block backdoor paths

- Pay attention to the direction of the arrow (causal path: don't want to condition on this)
- 4 possible permutations of arrows around a variable



- Are there any existing natural blocks?

Paths

Open (E and D are «d-connected»)	Blocked (E and D are d-separated)		Action (total effect)
$E \longrightarrow X1 \longrightarrow D$	$E \longrightarrow X1 \longrightarrow D$	Causal	Do not adjust for X1
$E \longleftarrow X1 \longrightarrow D$	$E \longleftarrow X1 \longrightarrow D$	Non-causal	Adjust for X1
$E \longleftarrow X1 \longleftarrow D$	$E \longleftarrow X1 \longleftarrow D$	Causal (reverse)	Switch E and D
$E \longrightarrow X1 \longleftarrow D$	$E \longrightarrow X1 \longleftarrow D$	Non-causal	Do not adjust for X1

Goal:

Want to keep all causal pathways open

Close the non-causal pathways (backdoor paths)

Example: Outside temperature and the risk of bone fracture in older adults



- **Bone fracture incidence** has been found to vary by **season** in Norway and in other countries, higher incidence in wintertime vs. summertime
- There is also a variation by **latitude**, in general a lower incidence at higher latitudes (in Sweden and in the rest of Europe), but no clear variation by latitude in Norway
- In Norway we see a higher incidence inland compared to the coast
- Can **outside temperature** be a «causal factor» in this pattern?

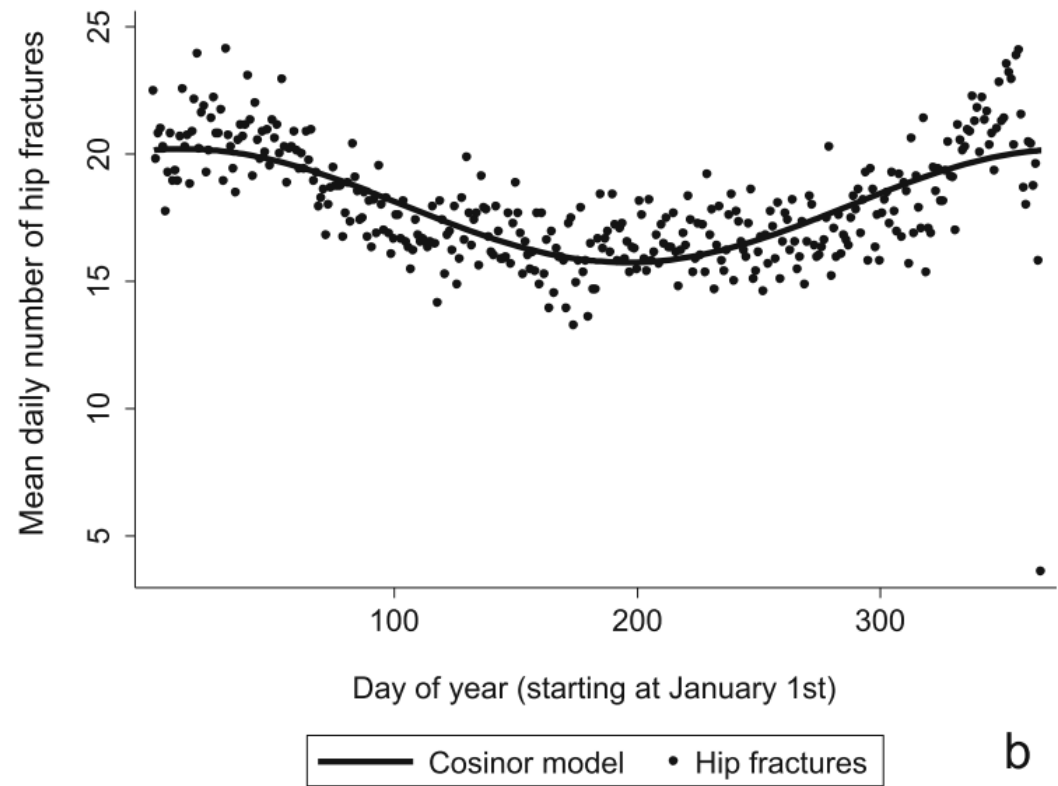
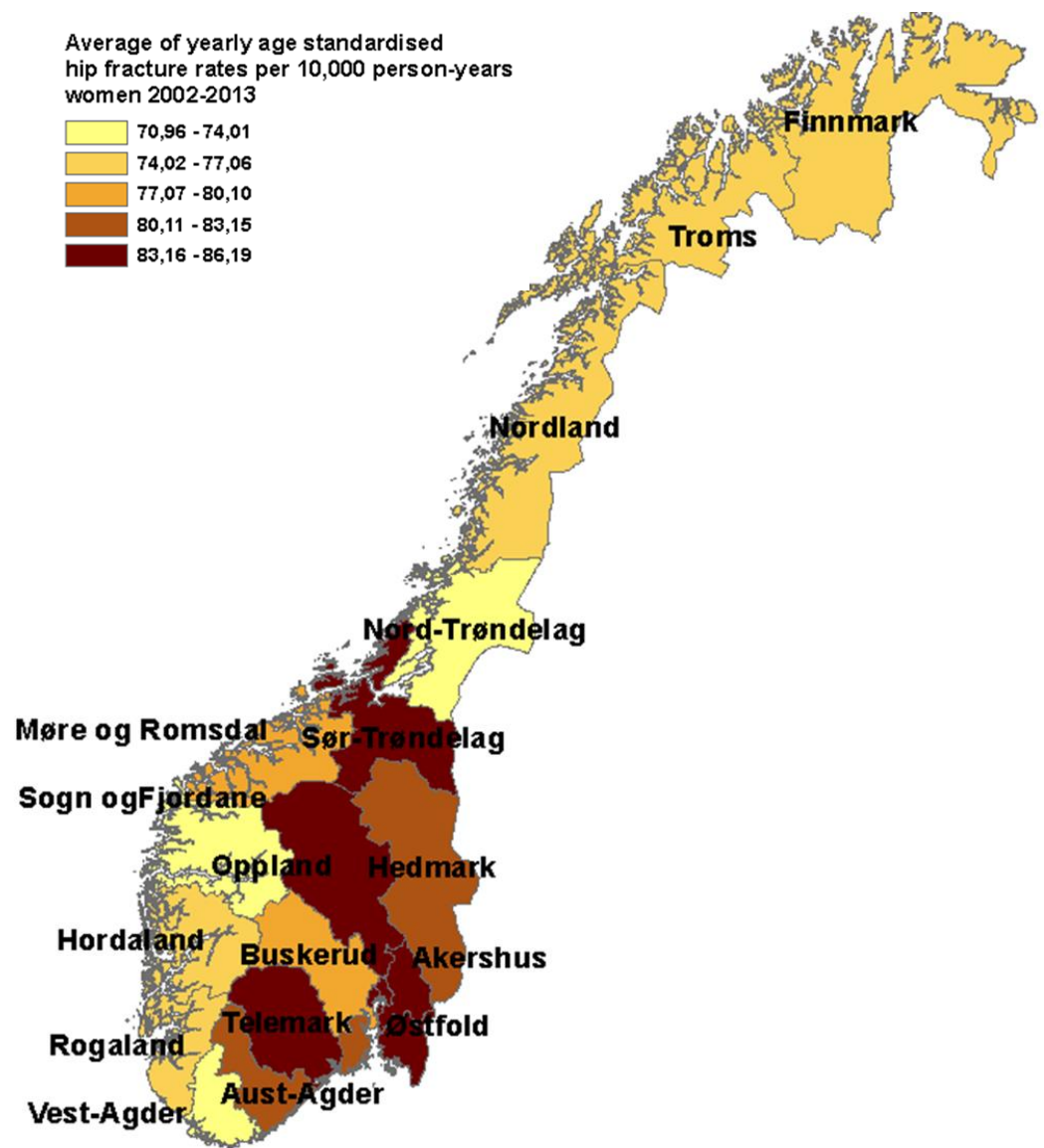
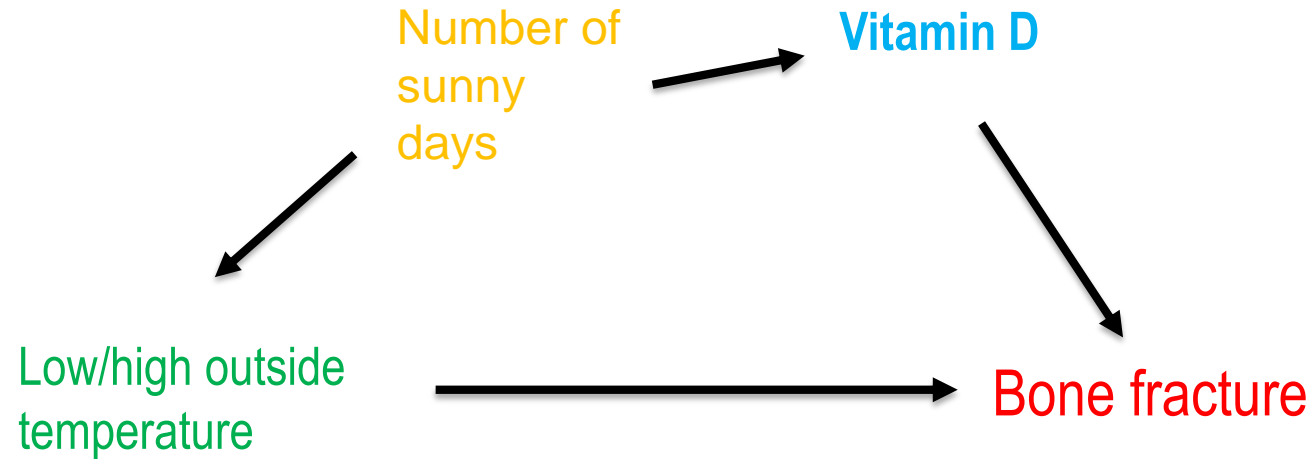
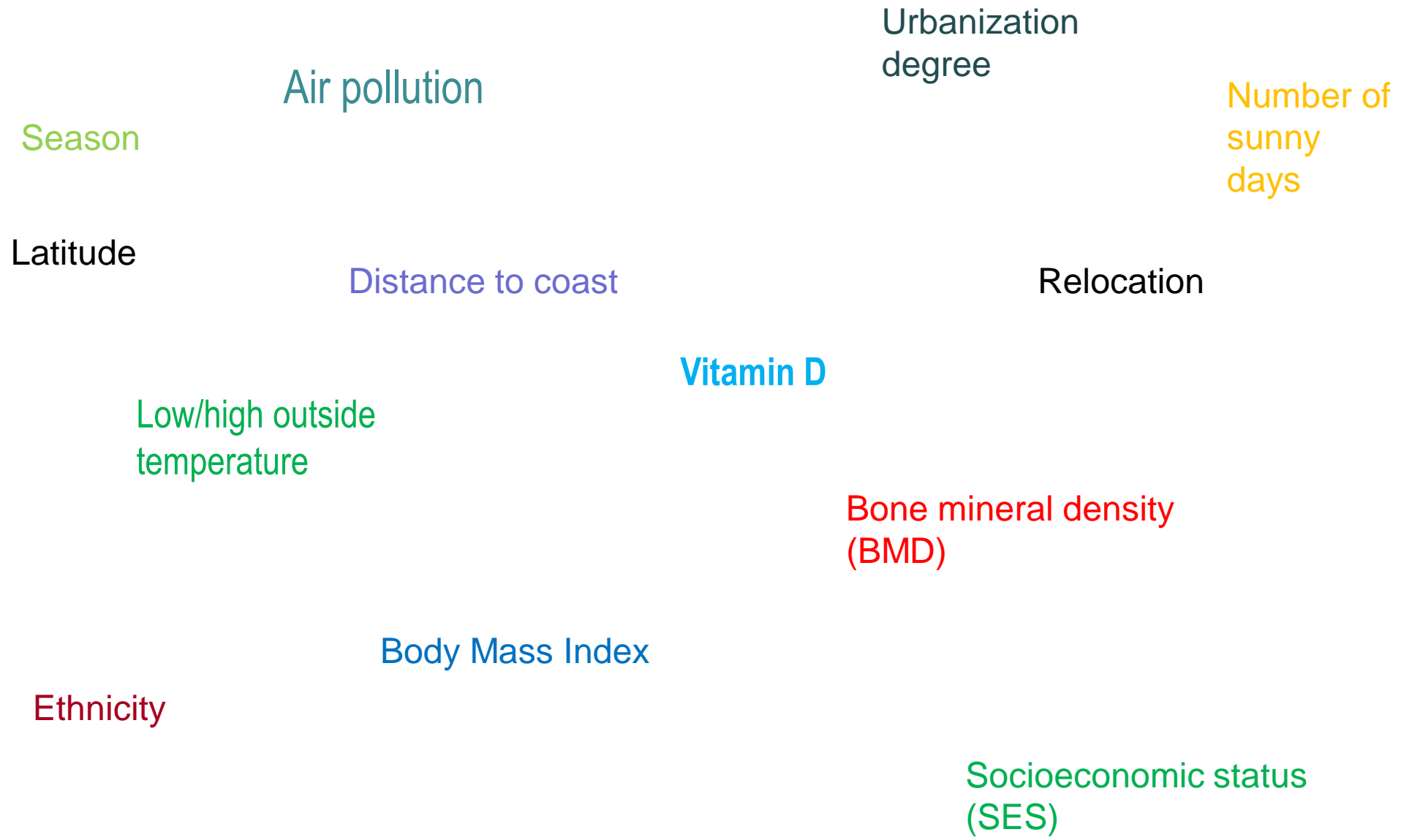


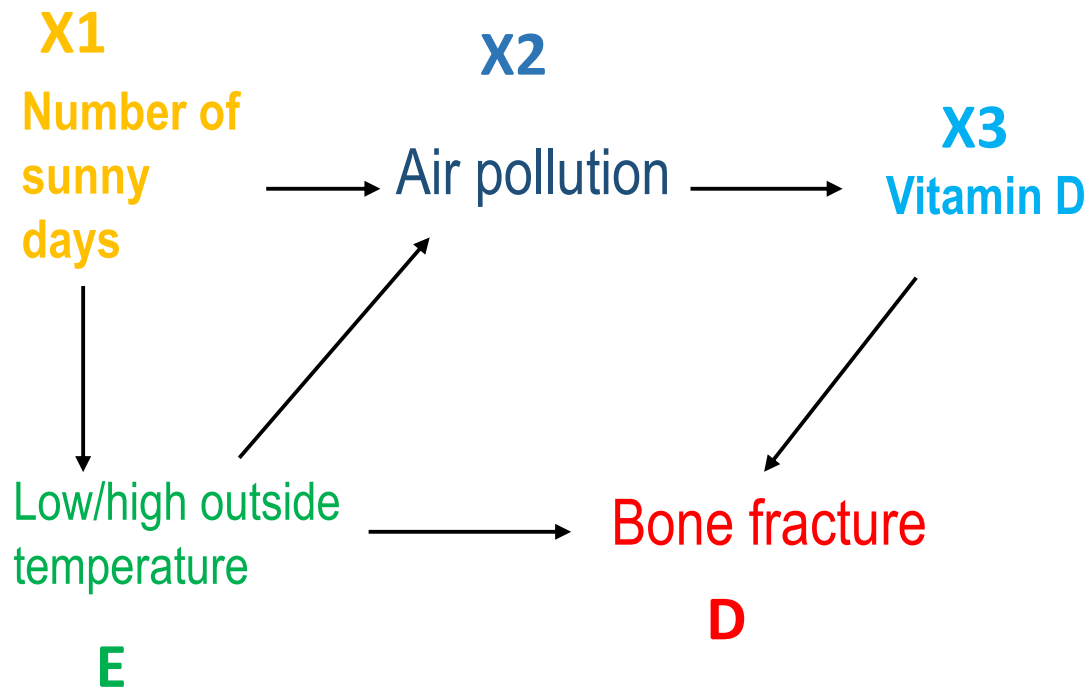
Fig. 2 Mean daily number of hip fractures during 1994–2008 (Norwegian patients aged 50–103 years) in **a** men and **b** women. A time series model (Cosinor model) is fitted. Norwegian Epidemiologic Osteoporosis Studies (NOREPOS)

Example: Outside temperature and the risk of bone fracture in older adults





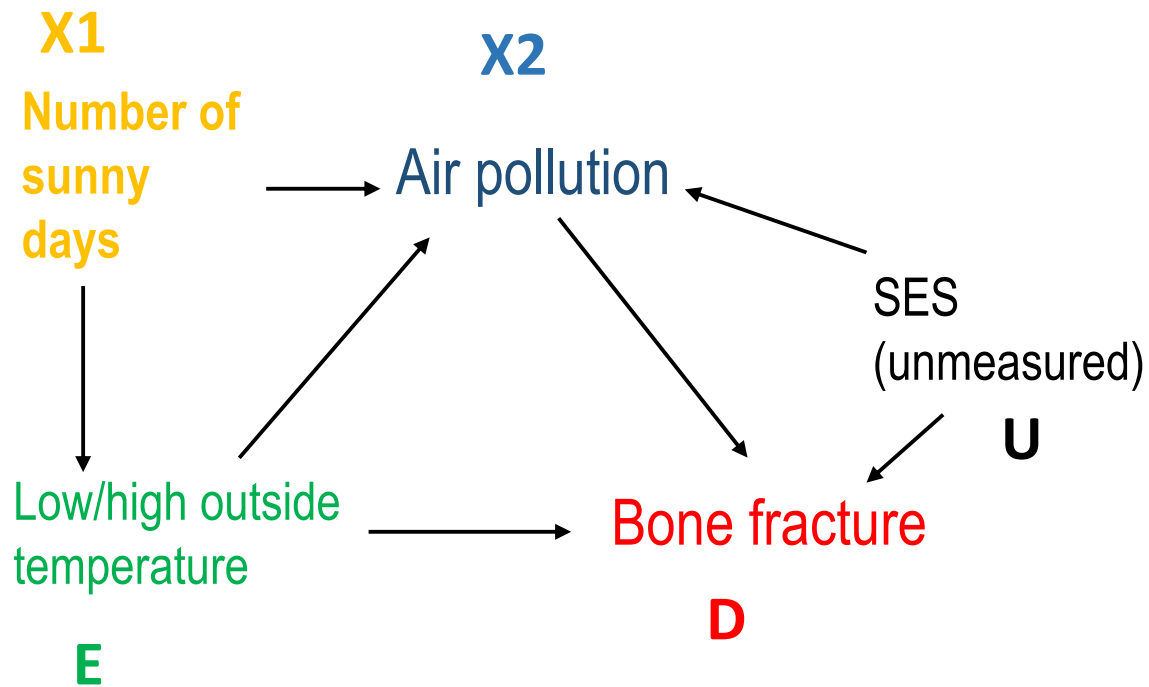
Exercise 1a: Temperature and the risk of bone fracture in older adults



Low temperature= Mean yearly temp < 10°C
High temperature= Mean yearly temp > 10°C

1. Write down the paths
2. Are they causal/non-causal, open, closed?
3. How would you get the
 1. total effect
 2. direct effect

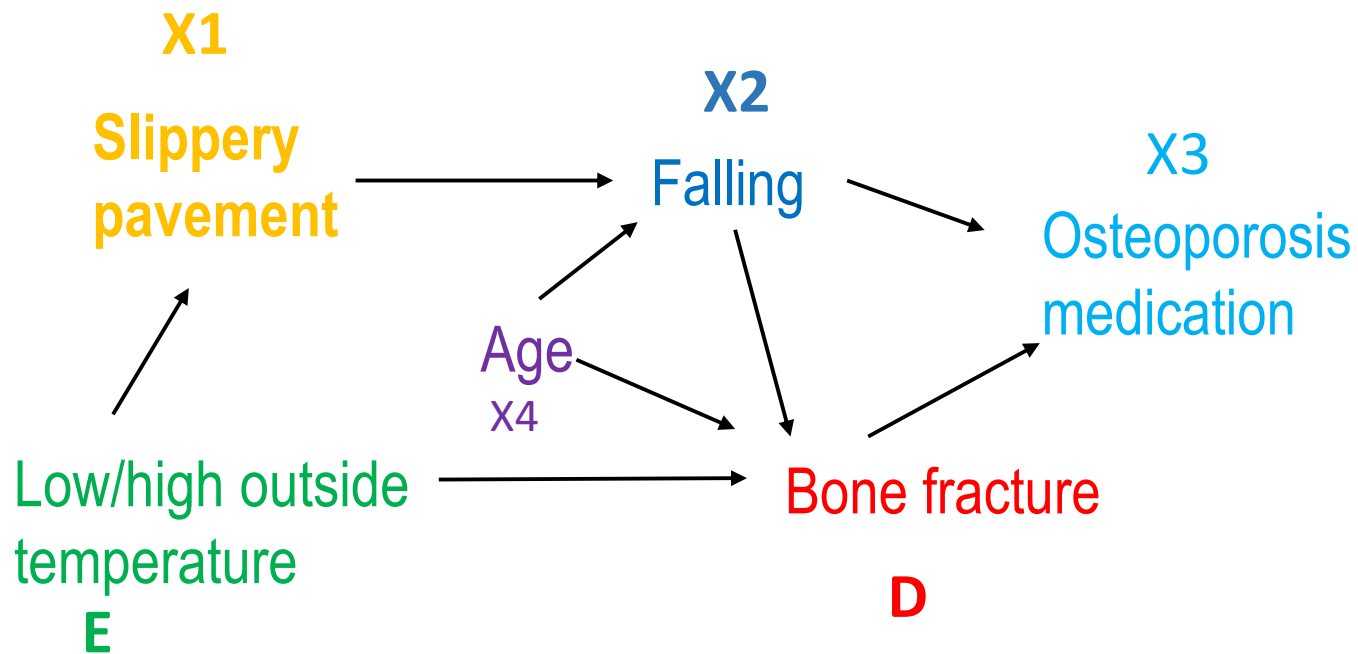
Exercise 1b: Temperature and the risk of bone fracture in older adults



Low temperature= Mean yearly temp < 10°C
High temperature= Mean yearly temp > 10°C

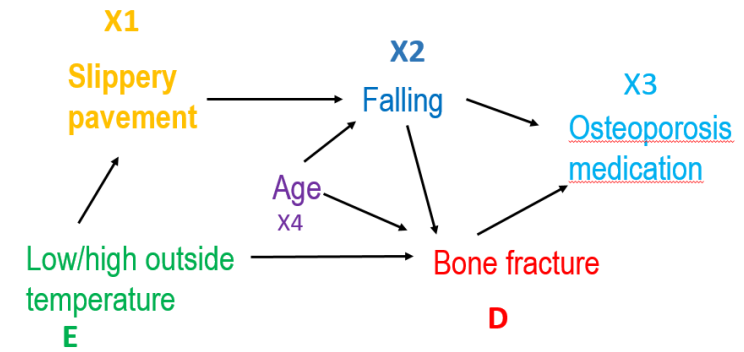
1. Write down the paths
2. Are they causal/non-causal, open, closed?
3. How would you get the
 1. total effect
 2. direct effect

Exercise 2. Temperature and the risk of bone fracture in older adults



1. Write down all the paths
2. Are they open or closed, causal or non-causal?
3. How would you get the total effect of Outside temperature on Bone fracture?
4. Optional: How would you get the direct effect ?

Hypothetical analysis



	Bone fracture				
	Yes	No	Total personyears	Rate	RD
Low outside temperature	84	9,916	10,000	0.0084	0.0
High outside temperature	84	9,916	10,000	0.0084	

What happens if you restrict on osteoporosis medication? (Will be covered in class)

How to select an **adjustment set**?

- **Adjustment set**: *minimum* set of variables to include in analysis in addition to our exposure and outcome
- By hand: Write down all paths between exposure and outcome, and between covariates, close the open non-causal paths
 - Can be difficult!
- Rather: **Use a program!**
 - The program will give a suggestion on the variables to include to obtain an unbiased association (if possible)

<http://dagitty.net/>

Welcome to DAGitty!

<http://dagitty.net/>

<p>Launch</p>  <p>Launch DAGitty online in your browser</p>	<p>Download</p>  <p>Download DAGitty's source for offline use</p>	<p>Learn</p>  <p>Learn more about DAGs and DAGitty</p>	<p>Code</p>  <p>The R package "dagitty" is available on CRAN or github</p>
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What is this?

DAGitty is a browser-based environment for creating, editing, and analyzing causal models (or causal Bayesian networks). The focus is on the use of causal diagrams for minimizing and other disciplines. For background information, see the "[learn](#)" page.

DAGitty is developed and maintained by [Johannes Textor](#) ([Tumor Immunology Lab](#) and [Sciences, Radboud University Nijmegen](#)). The algorithms implemented in DAGitty were co-developed by [Maciej Liśkiewicz](#) and [Benito van der Zander](#), University of Lübeck, Germany (see literature).

DAGitty development happens on [GitHub](#). You can download all source code from there.

How can I get help?

If you encounter any problems using DAGitty, or would like to have a certain feature implemented, please contact [johannes.textor {at} gmx {dot} de](mailto:johannes.textor@tumorimmunologylab.nl). Your feedback and bug reports are very welcome and contribute to the improvement of DAGitty for everyone. Past contributors are acknowledged in the [manual](#).

Is it free?

Because the main purpose of DAGitty is facilitating the use of causal models in empirical research, DAGitty is free software (both "free as in beer" and "free as in speech"). You can copy, redistribute, and modify it under the terms of the [general public license](#). Enjoy!

DAGitty development has been sponsored by the Leeds Institute for Data Analytics and the German Research Foundation (DFG), grant [273587939](#).

Versions

The following versions of DAGitty are available:

- [Development version](#)
Recent development snapshot. May contain new features, but could also contain new bugs.
- [Experimental version](#)
Most recent development snapshot. May not even work.
- [2.3: Released 2015-08-19](#)
- [2.2: Released 2014-10-30](#)
- [2.1: Released 2014-02-06](#)
- [2.0: Released 2013-02-12](#)
- [1.1: Released 2011-11-29](#)
- [1.0: Released 2011-03-24](#)
- [0.9b: Released 2010-11-24](#)
- [0.9a: Released 2010-09-01](#)

News on Twitter

[#dagitty](#)

Wolfhart Feldmeier Retweeted

 **Malcolm Barrett**
@malco_barrett

🎉 Now on CRAN: ggdag 0.1.0! Create and analyze tidy causal DAGs in #rstats using ggraph. Powered by @JohannesTextor's amazing dagitty pkg with graph 🙌 from ggraph by @thomasp85. #causalinference #dagitty malco.io/2018/03/28/ggd...

Draw, Analyze, Test

Diagram style

- classic
- SEM-like

View mode

- normal
- moral graph
- correlation graph

Coloring

- causal paths
- biasing paths
- ancestral structure

Effect analysis

- atomic direct effects

Legend

- exposure
- outcome
- ancestor of exposure
- ancestor of outcome
- ancestor of exposure and outcome
- adjusted variable
- unobserved (latent)
- other variable
- causal path
- biasing path

Summary

exposure(s) **Low/High outside temperature**

outcome(s) **Bone Fracture**

covariates **3**

causal paths **3**

Causal effect identification

Adjustment (total effect)

Minimal sufficient adjustment sets for estimating the total effect of Low/High outside temperature on Bone Fracture:

- Number_of_sunny_days

Testable implications

The model implies the following conditional independences:

- Bone Fracture \perp Number_of_sunny_days | Air_pollution, Low/High outside temperature
- Low/High outside temperature \perp Vitamin_D_intake | Air_pollution
- Number_of_sunny_days \perp Vitamin_D_intake | Air_pollution

[Export R code](#)

Model code

```
Vitamin_D_intake
Low%2FH%20high%20outside%20temperature
Air_pollution
Bone%20Fracture
Number_of_sunny_days
Air_pollution
Low%2FH%20high%20outside%20temperature
Vitamin_D_intake
Bone%20Fracture
```

(Textor, Hardt et al. 2011)

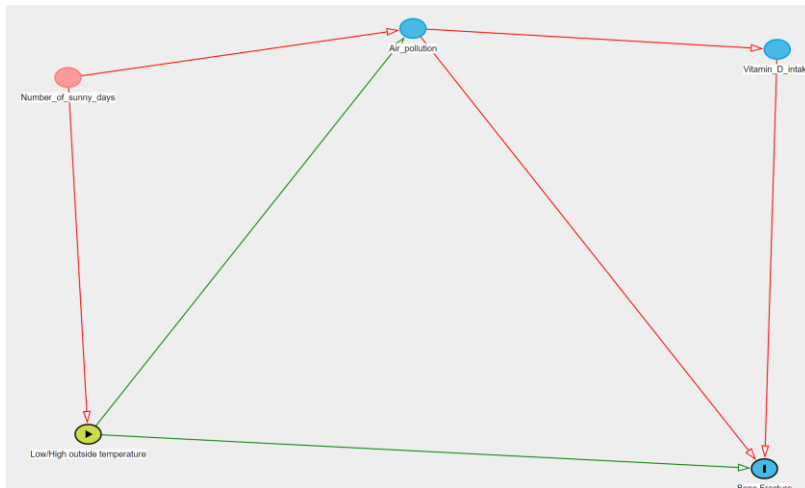
Draw model

- Draw new model
 - Model>New model, Exposure, Outcome
- New variables, connect
 - nnew variable (or double click)
 - c connect (hit c over V1 and over V2 to connect)
 - r rename
 - ddelete
- Status (toggle on/off)
 - uunobserved
 - aadjusted

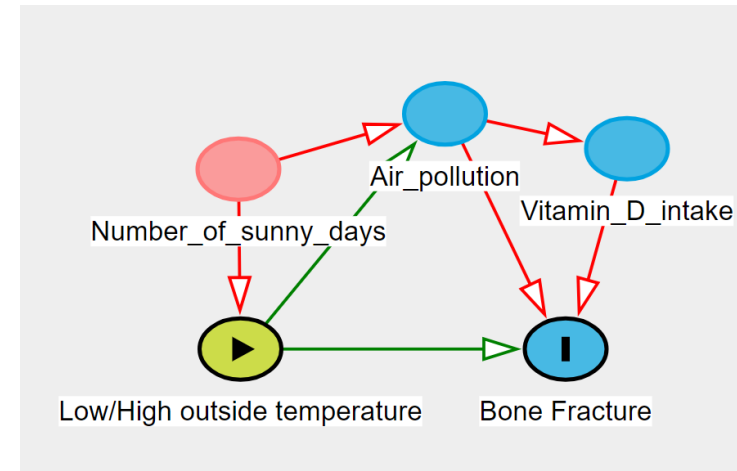
Export DAG

- Export to Word or PowerPoint
 - “Zoom” the DAGitty drawing first (*Ctrl-roll*)
 - Use “Snipping tool” or
 - use **Model>Export as PDF**

Without zooming



With zooming



Daggity: Draw all causal relationships

- Draw all variables/ factors that may influence your *outcome*
- Consider whether these factors also affect your *exposure*
- Are there any arrows between *cofactors*?
- Also put in common *ancestors of any two variables included*, also variables that are *unobserved*
- Remember: *Absence* of arrow is a strong statement
 - Omitting an arrow will explicitly state that there is no association between variables in *any* of your participants

- Now: Use Daggity to draw and analyse DAGs in your own research question.
- Next: Discussion of student examples
- Short summary